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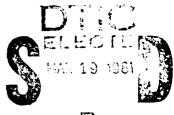
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# NORM2L

AN INTERACTIVE COMPUTER PROGRAM FOR ACOUSTIC NORMAL MODE CALCULATIONS FOR THE PEKERIS MODEL



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D.R.E.A. TECHNICAL MEMORANDUM 80/K



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DARTMOUTH N.S.

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NORM2L

AN INTERACTIVE COMPUTER PROGRAM FOR ACOUSTIC NORMAL MODE CALCULATIONS FOR THE PEKERIS MODEL

December 80

Approved by R. F. Brown Director / Underwater Acoustics Division

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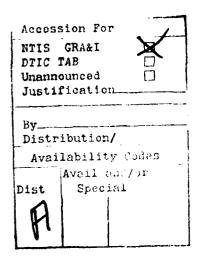
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#### **ABSTRACT**

The interactive computer program, NORM2L, calculates the discrete normal modes and acoustic propagation loss for the Pekeris model of the ocean. The Pekeris model is a simple two-layer model in which the two layers represent the seawater and seabed. For many shallow-water environments, the model is a reasonable approximation to the actual physical situation and can be used to investigate acoustic propagation at low frequencies.

For ease of future expansion and modification, the program NORM2L is written in modular form in FORTRAN. The results of NORM2L are compared with those of other computer programs.





#### RESUME

Le programme d'ordinateur interactif NORM2L sert à calculer les modes normaux discrets et la perte de propagation acoustique pour le modèle de Pekeris de l'océan. Le modèle de Pekeris est un modèle simple à deux couches dans lequel les deux couches représentent l'eau de mer et le fond de la mer. Pour plusieurs environnements en eau peu profonde, ce modèle est une approximation raisonnable de la situation réelle et peut servir à étudier la propagation des ondes acoustiques aux basses fréquences.

Pour en faciliter l'expansion et la modification futures, le programme NORM2L est écrit sous forme modulaire en langage FORTRAN. L'auteur compare les résultats du NORM2L à ceux des autres programmes d'ordinateur.

# TABLE OF CONTENTS

	Page No
ABSTRACT	ii
TABLE OF CONTENTS	iv
1. INTRODUCTION	1
2. THEORETICAL BASIS	4
<ul><li>2.1 The Pekeris Model</li><li>2.2 Method of Solution</li></ul>	4 10
3. PROGRAM DESCRIPTION	13
<ul><li>3.1 Program Structure</li><li>3.2 Important Variables</li><li>3.3 Testing and Verification</li></ul>	13 15 18
4. CONCLUSION AND RECOMMENDATIONS	22
TABLES	24
FIGURES	28
REFERENCES	31
APPENDICES	
A. USER'S GUIDE FOR PROGRAM NORM2L	33
A.1 Identification A.2 Hardware-Software Environment A.3 Input/Output A.4 Operational Instructions A.5 Restrictions and Limitations A.6 Functions and Subroutines A.7 Accuracy A.8 Memory Requirements A.9 Execution Times	34 34 35 38 41 42 44 45
B. SAMPLE TERMINAL INPUT/OUTPUT C. SAMPLE LINE PRINTER OUTPUT D. PROGRAM LISTING E. FUTURE MODIFICATIONS AND EXTENSIONS F. USER COMMENTS	47 51 55 69 71
DOCUMENT CONTROL DATA	73

#### 1 INTRODUCTION

NORM2L is an interactive computer program which calculates the discrete normal modes and propagation loss for the Pekeris [1] acoustic model described in section 2.1. Although this model is simple, it contains all the essential features of normal mode theory, and for many shallow water environments is a reasonable approximation to the actual physical situation.

The main reason for writing NORM2L was to have a convenient program for becoming acquainted with normal mode calculations. The interactive program and simple model allow rough answers to be obtained quickly and cheaply. Since many of the solutions are known analytically, the extensive calculations of a general normal mode program are not necessary. Also, the interactive nature of the program allows the user to see the results immediately. The user can then change the input parameters and look at the new set of results. In this way, the user can quickly get a feeling for the importance of the physical parameters.

Another reason for writing the program was to test new ideas and algorithms in normal mode theory in an easy to modify package. For example, to help verify that a numerical procedure is working or that a particular normal mode program has been implemented properly, the results from the analytic solutions of the Pekeris model can be compared with similar results from other normal mode programs which

obtain their results numerically. In one application a slightly modified version of NORM2L was found valuable in testing and debugging a normal mode program based on a two-ended shooting method [2,3]. In another application, not foreseen at the time NORM2L was written, the program was modified and some of the output used for mode enhancement in a preliminary analysis of some real data [4]. The present report does not discuss these applications, but restricts itself to a description of the program.

The main body of the report contains a general description of the model and program, with details relegated to the appendices. Section 2 contains the theoretical basis with a summary of the Pekeris model and a description of the algorithm used to calculate the normal mode wave numbers. Section 3 contains a general description of the program, its structure and important variables, and results of testing and verification. A number of tables are presented on wave numbers, mode functions, and propagation loss to be used as reference for checking the accuracy of new or other normal mode programs. In Section 4, the recommendations contain some possible future extensions and uses of the program.

Appendices A to D contain further details on the program. Appendix A is a user's guide for NORM2L with details on the hardware-software environment, input and output, operational instructions, restrictions and limitations, functions and subroutines, accuracy, memory

requirements, and execution times. Appendices B and C present sample input/output from the terminal and line printer, and Appendix D contains a program listing.

Appendices E and F are forward-looking, giving some anticipated modifications and extensions and a place for the user to add his comments and suggestions. Some of these changes will be incorporated in future versions of NORM2L.

#### THEORETICAL BASIS

### 2.1 The Pekeris Model

Figure 1 illustrates the environment described by the Pekeris [1] acoustic normal mode model. The model has a homogeneous layer of thickness h bounded above by a pressure release surface and bounded below by a homogeneous semi-infinite half-space of greater sound speed. The sound speeds  $\mathbf{c}_1$  and  $\mathbf{c}_2$  and the densities  $\mathbf{p}_1$  and  $\mathbf{p}_2$  are constants. To make the environment more realistic, the bottom layer has been given an absorption coefficient  $\mathbf{a}_2$ . A source at depth  $\mathbf{z}_s$  in the first layer is operating at frequency f. The problem is to calculate the propagation loss between the source and a receiver at depth  $\mathbf{z}_r$  and horizontal distance r from the source.

The greater sound speed of the bottom causes some of the acoustic energy to be totally reflected from the bottom. The successive reflections from the surface and bottom cause the water layer to act as a waveguide, and a standing wave pattern is set up in the depth direction. These standing waves are the normal modes. Near the source some of the energy strikes the bottom at angles less than the critical angle and is partially transmitted. This energy corresponds to the continuous spectrum of normal mode theory. Since this energy leaks out to the bottom after several bottom reflections, it is nearly always neglected in normal mode calculations. Like most normal mode programs, NORM2L

calculates only the discrete normal modes. This means that the model is not applicable when the source and receiver are separated by horizontal distances less than several water depths.

A standard reference for underwater acoustics is Tolstoy and Clay [5], although the formulae for the normal mode equations are scattered throughout the book. Chapter 9 of the newer book by Clay and Medwin [6] contains a fairly clear introduction to normal mode theory. Only the essential equations are presented here. Note that the formulation is in terms of the velocity potential, and that only the discrete modes are calculated.

For a frequency f (angular frequency  $\omega=2\pi f$ ) the normal modes are the eigenfunctions  $u_n(z)$  of the following differential equation

$$\frac{d^2 u_n}{dz^2} + \left[\frac{\omega^2}{c^2} - k_n^2\right] u_n(z) = 0 .$$
 (1)

Once the eigenvalue  $\mathbf{k}_n$  is determined (see below), the solutions  $\mathbf{u}_n$  for the two layer model are given as follows:

$$u_n(z) = A_n \sin(\gamma_{in} z)$$
,  $o \le z \le h$  (2a)

$$u_n(z) = (\rho_1/\rho_2) A_n \sin(\gamma_{1n}h) \exp[-\gamma_{2n}(z-h)], \qquad z>h$$
 (2b)

where

$$\gamma_{1n} = \left[\omega^2/c_1^2 - k_n^2\right]^{1/2} \tag{3a}$$

$$\gamma_{2n} = [k_n^2 - \omega^2/c_2^2]^{1/2}$$
 (3b)

and

$$A_n^{-2} = \frac{1}{2} \rho_1 h \left[ 1 - \frac{\sin(2\gamma_1 n^h)}{2\gamma_1 n^h} + \frac{\rho_1}{\rho_2} \frac{\sin^2(\gamma_1 n^h)}{\gamma_2 n^h} \right]$$
 (4)

The normalization factor  $A_n$  is determined from:

$$\int_{0}^{\infty} \rho(z) u_{n}(z) u_{m}(z) dz = \delta_{nm}$$
 (5)

where  $\delta_{\mbox{\scriptsize nm}}$  is the Kronecker delta function.

The conditions of continuity of pressure and particle velocity require that at the interface z=h:

$$\rho_1 u_n(h^{\dagger}) = \rho_2 u_n(h^{\dagger}) \tag{6a}$$

$$\frac{du_n(h^-)}{dz} = \frac{du_n(h^+)}{dz} \tag{6b}$$

Condition 6a has already been incorporated into the equation for  $\mathbf{u}_n$  . Condition 6b gives the equation used to determine  $\mathbf{k}_n$  ,

$$\tan \left\{ h \left[ \omega^2 / c_1^2 - k_n^2 \right]^{1/2} \right\} = -\frac{\rho_2}{\rho_1} \left[ \frac{\omega^2 / c_1^2 - k_n^2}{k_n^2 - \omega^2 / c_2^2} \right]^{1/2}$$
 (7)

Foliation of this equation leads to a set of discrete values for  $\kappa_n\colon$ 

$$\omega/c_1 > k_1 > k_2 > ... > k_N > \omega/c_2$$
 (8)

If there is attenuation in the bottom, the wave number of the sound speed in the bottom can be written as

the complex number  $k_B = \omega/c_2 + ie$ . Usually e is quite small in comparison to  $\omega/c_2$  and perturbation theory can be used [7]. Then,

$$k_n \to k_n + i \delta_n \tag{9}$$

where,

$$\delta_{n} = e^{\frac{\omega_{n}^{2}}{c_{2}k_{n}}} \int_{h}^{\infty} |u_{n}(z)|^{2} dz$$
 (10)

For the two layer model the integral can be evaluated, giving

$$\delta_{n} = e^{\frac{\omega \rho_{1}^{2} \Lambda^{2}}{2\rho_{2} c_{2}^{k} n^{\gamma} 2n}}$$
 (11)

Note that the absorption coefficient a<sub>2</sub> is usually given as dB per unit length referenced to 1 kHz. Since the attenuation is assumed to be linearly dependent on the frequency, then e is given by

$$e = a_2 (f/1000) (ln 10)/20$$
 (12)

and has units of inverse length, the same as the wave number.

The units are usually called nepers per unit length.

There are a number of conventions for what is meant by a unit source. The one used here will define a source of strength Q as one in which the pressure  $p(\underline{x})$  near the source at  $\underline{x}_0$  is given by

$$p(\underline{x}) = Q |\underline{x} - \underline{x}_0|^{-1} e^{ik_0} |\underline{x} - \underline{x}_0|$$
 (13)

where  $k_0 = \omega/c(\underline{x}_0)$ . The pressure due to the discrete modes

is then given by:

$$p(\underline{x}) = i\pi Q\rho(z) \sum_{n=1}^{N} u_n(z_0) u_n(z) H_0^{(1)}(k_n r)$$
(14)

and the propagation loss relative to unit distance, defined by

$$PL = -10 \log_{10} |p(\underline{x})/p(\underline{x}_1)|^2$$
 (15)

where  $|x_1-x_0| = 1$ , is given by

$$PL = -10 \log_{10} |\pi_{\rho}(z)| \sum_{n=1}^{N} u_{n}(z_{0}) u_{n}(z) H_{0}^{(1)}(k_{n}r)|^{2}$$
(16)

This formula is valid for all depths z [8], although most authors say it is valid only in layer one.

For  $k_{n}r$  large (and no attenuation in the bottom), the expression for the intensity  $\left\lceil p\right\rceil^{2}$  can be written as,

$$|p(x)|^{2} = |C|^{2} \sum_{n=1}^{N} |u_{n}(z_{0})u_{n}(z)|^{2} (2/\pi k_{n}r)$$

$$+ |C|^{2} \sum_{n\neq m}^{N} u_{n}(z_{0})u_{n}(z)u_{m}(z_{0})u_{m}(z) \frac{2}{\pi r(k_{n}k_{m})^{1/2}} e^{i(k_{n}-k_{m})r}$$
(17)

where C =  $i\pi Q_{\rho}(z)$ , and the Hankel function has been replaced by its asymptotic form

$$H_0(k_n r) \approx (2/\pi k_n r)^{1/2} e^{i(k_n r - \pi/4)}$$
 (18)

Notice that only the second term of (17) contains the oscillating trigonometric terms. There are several reasons for expecting this term to be small. First, if the r term in the denominator is removed, the average value of the term

(as a function of range) is zero. Moreover, as a function of z, the mode functions should appear more or less with random amplitudes and signs. Thus the main features of propagation loss are contained in the first term only. In addition, any source will have some frequency spread, which will smear out the fluctuations in the second term. If the intensity is calculated using only the first term, a very smooth function is obtained, from which a more meaningful comparison of various source and receiver depths and various ranges can be made.

This intensity gives rise to what is called the incoherent propagation loss:

IPL = -10 
$$\log_{10} \{ (\pi \rho(z))^2 \sum_{n=1}^{N} |u_n(z_0)u_n(z)H_0^{(1)}(k_n r)|^2 \}$$
 (19)

The incoherent propagation loss should be used cautiously for deep water since the regions of high and low intensity are averaged out. In shallow water it is a useful quantity and for broadband sources more meaningful than the coherent propagation loss PL.

Since the acoustic energy is trapped by the waveguide, the propagation loss as a function of range tends to behave as cylindrical spreading. It is sometimes convenient to remove this geometrical term by subtracting 10 log (r) from the propagation loss. Another geometrical factor which can be subtracted is the water depth correction, 10 log(h). This corresponds to the spreading of the acoustic energy

throughout the water column, and is closely related to the spherical spreading of the acoustic energy near the point source. The remainder term contains the losses due to the depth dependence of the propagation loss and losses due to absorption by the bottom. If there is no attenuation in the bottom layer, the remainder term will be constant with range. In the printout for the program (Appendix C) the incoherent propagation loss with cylindrical spreading and water depth correction removed appears under the heading INCOH-GEOM.

The excitation of a given mode n by a source at  $\label{eq:constraint} \text{depth } z_0 \text{ will be defined to be}$ 

$$\mathbf{E}_{\mathbf{n}} = \mathbf{u}_{\mathbf{n}}(\mathbf{z}_{\mathbf{0}}) \tag{20}$$

This is the coefficient of the n-th term in the sum for the pressure, see Eq.(14).

### 2.2 Method of Solution

To obtain the eigenvalues  $\mathbf{k}_n$  of the mode equation (1), the transcendental equation (7) must be solved. To facilitate the solution two dimensionless quantities are defined:

$$y_n = h[\omega^2/c_1^2 - k_n^2]^{1/2}$$
 (21)

and

$$b = (h\omega/c_1) \left[1 - c_1^2/c_2^2\right]^{1/2}$$
 (22)

Then equation (7) can be written as,

$$\tan y_n = -(\rho_2/\rho_1) y_n [b^2 - y_n^2]^{-1/2}$$
 (23)

or equivalently,

$$y_{n} = n\pi - \tan^{-1} \frac{(\rho_{2}/\rho_{1})y_{n}}{[b^{2}-y_{n}^{2}]^{1/2}}$$
 (24)

A Newton-Raphson iteration method is used to solve Eq. (24) for  $y_n$ . To first get a feeling for the results, a graphical solution to Eq.(23) can be obtained. This is illustrated in Figure 2 for the case of three modes. Notice that the roots  $y_n$  must occur on the negative branch of the tangent function or

$$(n - \frac{1}{2}) \pi < y_n < n\pi$$
 (25)

for n=1,2,...,N, where

$$N = [[\frac{1}{2} + \frac{b}{\pi}]]$$
 (26)

and the notation [[x]] means the greatest integer less than or equal to x. In terms of the environmental input parameters Eq.(26) becomes

$$N = \left[ \left[ \frac{1}{2} + (2hf/c_1) \left( 1 - c_1^2/c_2^2 \right)^{1/2} \right] \right]$$
 (27)

Also, since the right hand side of Eq.(22) is monotonically decreasing, it follows that successive values of  $y_n$  differ by less than  $\pi$ . So  $y_n$  is constrained by

$$(n - \frac{1}{2}) \pi < y_n < \min \{n\pi, b, y_{n-1} + \pi\}$$
 (28)

For the Newton-Raphson method we use the function

F(y) defined by

$$F(y) = y + \tan^{-1} \left[ \frac{\rho_2}{\rho_1} \frac{1}{(b^2 - y^2)^{1/2}} \right]$$
 (29)

The derivative of F is then given by:

$$F'(y) = 1 + \frac{(\rho_2/\rho_1)}{(b^2 - y^2)^{1/2} \{1 + [(\rho_2/\rho_1)^2 - 1](y/b)^2\}}$$
(30)

and an improved estimate of  $\mathbf{y}_{n}$  is obtained from the Newton-Raphson iteration formula:

$$y_n^{(i+1)} = y_n^{(i)} - F(y_n^{(i)}) / F'(y_n^{(i)})$$
 (31)

In the numerical procedure we must ensure that at each iteration the new value for  $\boldsymbol{y}_n$  remains in the range

$$(n - \frac{1}{2}) \pi < y_n^{(i)} < \min \{n\pi, b\}$$
 (32)

Once  $\boldsymbol{y}_n$  has been determined, the wave number is given by

$$k_{n} = \left[\omega^{2}/c_{1}^{2} - y_{n}^{2}/h^{2}\right]^{1/2} \tag{33}$$

The mode functions and propagation loss, etc., can then be calculated from the equations of Section 2.1.

#### 3. PROGRAM DESCRIPTION

### 3.1 Program Structure

The program NORM2L is written in modular form for ease of expansion and modification. An attempt has been made to remain close to standard Fortran, although for input and output some straying did occur. In particular, for input of data, free field formatting was used; and for printing of text, quotes were often used instead of the Hollerith specification. A simplified flowchart of NORM2L is given in Figure 3, and the interaction of the subroutines is depicted in the tree structure of Figure 4. Appendix A is a User's Guide for program NORM2L with details on the hardware-software environment, input/output, operational instructions, restrictions and limitations, functions and subroutines, accuracy, memory requirements, and execution times.

Below is a list of the subroutines and COMMON blocks and a one line description of their functions. A short but more detailed description of the functions and subroutines appears in Appendix A.6. The COMMON blocks are discussed further in Section 3.2.

# List of Modules and COMMON Blocks

### (a) Modules included in NORM2L

NORM2L	Main program. Driver program for I/O
NMODES	Calculates modes by calling MODE
MODE	Calculates eigenvalue for a single mode.
ATTENU	Calculates attenuation for the modes.
MODFUN	Prints modal functions at 12 depths
WFUNCT	Calculates mode functions at specified depths
UN	Evaluates a mode function at a specified depth
PLOSS	Propagation loss I/O routine
EXCITE	Calculates mode excitations for a <b>specified</b> source depth
PROPLO	Calculates propagation loss in dB//unit length
VPHI	Calculates velocity potential at the specified receiver depth
HANKO1	Evaluates the asymptotic Hankel function

# (b) DEC-20 subroutines (not included)

DATE	Returns	current	date
TIME	Returns	current	time

### (c) COMMON blocks

/CNTLIO/	I/O control. Contains logical unit numbers.
/ENVIRN/	Environmental and derived quantities
/EIGENF/	Eigenvalues and normalization constants
/CNTLNM/	Control parameters for calculating modes

# COMMON block usage:

COMMON Block	Modules that use the Block
/CNTLIO/	NORM2L, NMODES, MODES, PLOSS
/ENVIRN/	NORM2L, ATTENU, MODFUN, WFUNCT, PLOSS, VPHI
/EIGENF/	NORM2L, ATTENU, WFUNCT, PLOSS, VPHI
/CNTLNM/	NORM2L, NMODES, MODES

# 3.2 Important variables

# 3.2.1 Variables in COMMON blocks

# COMMON /ENVIRON/

Quantity	Variable name	Default value	Description
h	Н	100.	thickness of first layer
c <sub>1</sub>	C 1	1500.	sound speed in first layer
P 1	RHO 1	1.0	density of first layer
c 5	C2	1800.	sound speed in bottom layer
P2/P1	RHORAT	2.0	ratio of densities
e	ATTN	a=0.2	attenuation in bottom layer at given frequency
$\omega = 2 \pi f$	OMEGA	f=100.	angular frequency
$k_1 = \omega/c_1$	A K 1		wave number in first layer
k <sub>2</sub> = ω/c <sub>2</sub>	AK2		wave number in bottom layer

# COMMON /CNTLNM/

Variable name	Default value	Description			
MAX	20	maximum number of iterations allowed in the Newton-Raphson procedure			
TOL	1.0E-8	the tolerance desired in computing $\mathbf{y}_{n}$			
*NMIN	1	first mode to be calculated			
NMA X	50	maximum number of modes that can be calculated			
*VMIN	c 1	minimum phase velocity of modes			
*VMAX	°2	maximum phase velocity of modes			

 $<sup>\</sup>mbox{\tt\#}$  Treated as constants in this version. "Reserved for future expansion".

### COMMON /EIGENF/

Quantity	Variable name	Description		
N	NM	The number of modes actually calculated		
k <sub>n</sub>	AKM(50)	Array containing wave numbers of the modes		
An	ANM(50)	Array containing normalizations of the mode functions		
δn	ATN(50)	Array containing imaginary part of the wave numbers		

#### COMMON /CNTLIO/

	Logical	Current impleme	entation
File type	variable	Logical file	Device
Input	II	5	Terminal
Output	IT	5	Terminal
Output	10	3	Line printer

There are three logical files for input/output although in the current version two of these are identical. Variable names are used rather than numbers to allow for compatibility with other computers and other input/output devices. For example, on DEC's PDP-1134 computer the logical file numbers are 7, 7, and 6 respectively. Only one data statement needs to be changed. It may even be possible to run the program in batch mode by letting II correspond to the card reader, IT to some arbitrary file, and IO to the line printer.

3.2.2 Other important variables

Quantity	Variable name	Default value	Description
0,701	CRAT	1.2	ratio of sound speeds
5 9	RHO2	ρ <sub>2</sub> /ρ <sub>1</sub> =2.	density in bottom layer
а	ALPRAT	0.2	attenuation coefficient in bottom layer (dB/length // 1kHz)
f	FREQ	100.	frequency
z <sub>C</sub>	ZS	h/2	source depth
7.	ZR	h/2	receiver depth
r	R		range of receiver
	RMIN	10000.	minimum range for propagation loss (PL) calculations
	DELR	10000.	range increment for PL calculations
	NRNG	10	number of range increments for PL calculations
<sup>v</sup> n	VPHASE		phase velocity for mode n
PL	PL		<pre>propagation loss in dB   (relative to unit distance)</pre>
IPL	IPL		incoherent PL in dB
r.IPL	RCOHI		IPL with cylindrical spreading removed
π	PI		Greek pi (3.14159265)
h w/cj	HOMC		useful dimensionless quantity
b, b <sup>c</sup>	B, BSQ		useful quantity for determining eigenvalues (see Eq.22)

#### 3.3 Testing and Verification

To verify that the computer program was giving accurate answers, its output was compared with two other sources: a HP-67 programmable hand calculator program and a normal mode computer program by Bartberger and Ackler [9] (to be called BANORM in this report). The HP-67 program computes only the eigenvalues using an algorithm similar to the one described in Section 2.2, but the calculator carries about 10 significant digits, compared with about 8 for the TEC-20 computer; thus its solution will be regarded as exact. The program BANORM is a general normal mode program which calculates eigenvalues, mode functions and propagation loss for more complicated sound speed and density profiles than the Pekeris model. It was chosen for comparison because it was available, and because the CDC 6400 computer on which it was implemented had a precision of 14 significant digits. The program used a numerical integration of the differential equation, so its accuracy was not known beforehand. However, as will be seen, its eigenvalues seemed correct so its mode functions and propagation loss were assumed to also be correct. In the discussion below, the eigenvalues from the HP-67 program and the eigenvalues, mode functions and propagation loss from BANORM are compared with the corresponding values from NORMAL.

Several modifications to the normal mode program

BANORM were necessary before the results could be compared. First, the correction to the sound speed profile due to the earth's curvature had to be removed. Removal of the curvature caused the WKB approximation procedure to fail, so an additional modification was made. Another correction removed was the additional propagation loss due to volume absorption in the water column. One difference which could not be removed was the treatment of absorption in the bottom layer. Program BANORM treats the absorption "exactly" by using an imaginary value for the wave number, whereas in NORM2L the absorption is treated as a perturbation. The two programs should give identical results for the case where there is no attenuation in the bottom. To facilitate comparison of results BANORM was modified to accept input and print output in metric units, although the internal calculations were performed, as before, in yards. The values in the tables have been modified using the exact conversion factors as

$$k_n \rightarrow k_n/(0.9144)$$
 $u_n(z) \rightarrow (-1)^{n+1}(0.9144)^{-1/2}u_n(z)$ 
 $PL \rightarrow PL + \log_{10}(0.9144)$ 

Table I shows the results from the HP-67 two layer program, with the default values for the model. These values should have about 9 significant figures accuracy and were used to check output from the computer program. A comparison

with the results shown in Appendix B shows excellent agreement, with eight digits accuracy in  $\mathbf{k}_{\mathrm{n}}$ .

Table II compares the eigenvalues  $k_{\hat{n}}$  calculated by NORM2L and BANORM for the cases of no attenuation and attenuation equal to 0.2 dB/m//1 kHz. The results of the HP-67 calculation are repeated for easy comparison. For no attenuation all three methods agree to about eight significant digits, and the HP and CDC results agree to the full nine. Since the HP program did not calculate the mode functions or propagation loss, BANORM was used as the reference for judging the accuracy of NORM2L. When the bottom absorption is non-zero, the exact solution shows a shift in the real part of the eigenvalue as well as the introduction of an imaginary part. The shift in the real part is less than the imaginary part, however. In the example the real parts of  $k_n$  agree to about six figures accuracy for the exact and perturbation calculations. The imaginary parts agree to about three figures accuracy, or about the seventh decimal place. Notice that the imaginary part, though small, increases with increasing mode number a factor of about 50 in the seven modes.

The mode functions are compared at two depths in Table III. The answers agree to about six decimal places. Eresumably, handred is the more accurate because of the greater accuracy in the wave numbers  $\mathbf{k}_n$ . As is quite common in numerical approximations, the eigenfunctions are less

accurate than the eigenvalues. When attenuation is considered, the mode functions agree to only four digits.

NORM2L and BANORM for source and receiver at mid-depth, with bottom absorption both present and absent. The values for the average or incoherent propagation loss (IPL) are considerably more in agreement than those for the coherent propagation loss (PL) - five digits compared with four for no absorption, and four digits compared with three digits for attenuation coefficient a=0.2. For the IPL there seems to be a consistent bias with BANORM giving values low by 0.0002 dB for a=0 and by 0.002 for a=0.2. At present no explanation can be given for this bias.

In summary, for no bottom absorption the wave numbers as calculated by NORM2L are probably accurate to eight significant digits, the mode functions accurate to about six digits, and the propagation loss to five digits. When absorption is included as a perturbation, the accuracy of the results is degraded, but the propagation loss remains accurate to better than 0.1 dB.

#### 4. CONCLUSIONS AND RECOMMENDATIONS

NORM2L was written to provide an interactive computer program for calculating the discrete normal modes and acoustic propagation loss for the Pekeris model of the ocean. Although the model is simple, it contains all the essential features of normal mode theory, and for many shallow water environments is a reasonable approximation to the actual physical situation. The simple model has the advantage that the extensive calculations of a general normal mode program are not necessary and an interactive program can be used. The interactive nature of the program makes it useful for sensitivity studies since the user can see the results immediately, change the input parameters and look at a new set of results. The user can then quickly get a feeling for the importance of the physical parameters.

In practice the program has proved to be very useful as a learning tool for normal mode calculations and for sensitivity studies. In view of the utility of the program it is recommended that certain extensions and improvements be made to the program. Certain improvements could be made to the present program to provide more options and improve output to include graphing of mode functions and propagation loss. These are listed in Appendix E. Some extensions could be made to the model to improve its usefulness for sensitivity studies by allowing for a more realistic environment. For example, propagation loss will

be affected by the presence of shear waves in the bottom or scattering from a rough surface or bottom. These could be included as perturbation effects to be added to the present program, or treated more rigorously in an extended program. If the acoustic field is needed near the source, the continuous modes are important and should be calculated. Range dependence could be included in the model to allow for a sloping bottom or changing bottom properties. This could be incorporated in an approximate manner in the adiabatic approximation (no mode coupling), or more exactly by including mode coupling effects.

Table I. Eigenvalues obtained using the Newton-Raphson iteration procedure

mode	iteration	s y <sub>n</sub>	k <sub>n</sub>	<sup>v</sup> n
1	10	2.894719966	0.417877606	1503.594646
2	9	5.805255120	0.414836757	1514.616340
3	9	8.740763033	0.409657833	1533.764231
4	8	11.70219503	0.402200817	1562.201031
5	7	14.68458504	0.392295718	1601.645144
6	7	17.67884983	0.379743941	1654.584742
7	8	20.66772252	0.364340718	1724.535581

The results shown are for the HP-67 program with the default parameters h=100, c<sub>1</sub>=1500,  $\rho_1$ =1, c<sub>2</sub>/c<sub>1</sub>=1.2,  $\rho_2$ /  $\rho_1$ =2.0, and f=100. The results were obtained by a Newton-Raphson procedure which iterated until successive approximations to  $y_n$  differed by less than 1.0E-9. The initial approximation was  $y_n$ =(n-1/2) $\pi$ .

Table II. Comparison of Wave Numbers

Mode	Exact	NORM 2L		Bartberger-Ackler		
	k <sub>n</sub>	<sup>k</sup> n	δn	k <sub>n</sub> (a=0)	$k_n(a=.2)$	$\delta_{n}(a=.2)$
1	.417877606	.41787760	.23081(-5)	.417877606	.417877551	.23066(-5)
2	.414836757	.41483675	.85045(-4)	.414836757	.414836565	.84998(-4)
3	.409657833	<b>.4</b> 0965783	.17149 (-4)	.409657833	.409657434	.17141(-4)
4	.402200817	.40220081	. 27377 (-4)	.402200817	.402200241	. 27364 (-4)
5	.392295718	.39229571	.39711(-4)	.392295718	.392294853	.39688 (-4)
6	.379743941	.37974394	.57252(-4)	.379743941	.379742482	.57202(-4)
7	.364340718	.36434072	.94016(-4)	.364340718	.364336855	.93761(-4)

The default parameters given with Table I have been used for the calculations. The exact values are from the HP-67 program.

Table III. Comparison of Mode Functions

At depth 50

mode	NORM2L	BANORM(a=0)	BANORM(a=0.2)
1	.1348502	.1348504	.1348530
2	.3228419(-1)	.3228438(-1)	.3227565(-1)
3	1290802	1290816	1290872
4	5761266(-1)	5761346(-1)	5760186(-1)
5	.1203002	.1203022	.1203128
6	.7630017(-1)	.7630139(-1)	.7628658(-1)
7	1085481	1085494	1085981

At depth 25

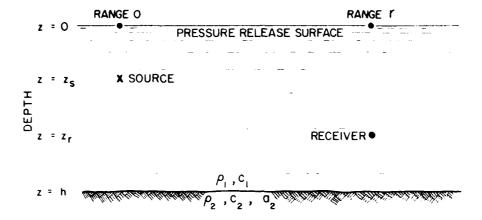
mode	NORM2L	BANORM(a=0)	BANORM(a=0.2)
1 2 3 4 5 6	.8997515(-1) .1354220 .1119586 .2949192(-1) 6969622(-1) 1322287 1236168	.8997537(-1) .1354228 .1119598 .2949233(-1) 6969738(-1) 1322308 1236184	.8997854(-1) .1354246 .1119571 .2948582 6970512 1322377 1236284

The default parameters given with Table I were used for the calculations.

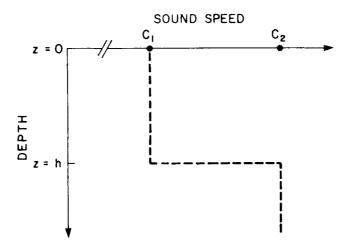
Table IV. Comparison of Propagation Loss.

a=0			5.440		
	NORMAL			BANORM	
r	PL	IPL	PL	IPL.	
10000 20000 30000 40000 50000 60000 70000 80000 90000	57.4530 62.1264 62.9224 64.3649 81.6223 66.5136 73.5068 64.2857 72.6916 64.7800	58.0333 61.0436 62.8047 64.0539 65.0230 65.8148 66.4842 67.0642 67.5757 68.0333	62.1259 62.9221 64.3650 81.6213 66.5127 73.5066 64.2868 72.6934	58.0331 61.0434 62.8043 64.0537 65.0228 65.8146 66.4841 67.0640 67.5755 68.0331	
a=0.2					
	NORM2L		BANO	BANORM	
r	PL	IPL	PL	IPL	
10000 20000 30000 40000 50000 60000 70000 80000 90000	58.3779 64.9796 65.4292 70.6964 76.3537 75.9126 74.7604 74.8863 74.8971 74.4043	60.0250 64.2338 66.8262 68.7062 70.1800 71.3920 72.4229 73.3220 74.1222 74.8458	65.1382 65.4717 70.6569 76.4301 76.0060 74.7096 74.7803 74.8337	60.0225 64.2318 66.8244 68.7044 70.1782 71.3903 72.4211 73.3202 74.1203 74.8439	

The standard environmental model is used; source and receiver are at mid-depth. Pi is the coherent propagation loss, IPL is the incoherent propagation loss, and a is the attenuation coefficient.



(a) The layer structure: densities  $\rho_1$  and  $\rho_2$ , sound speeds  $c_1$  and  $c_2$ , and bottom absorption  $a_2$  are all constants, and  $c_1$  <  $c_2$ . The source and receiver are at depths  $z_s$  and  $z_r$  respectively and separated by horizontal distance r.



(b) The sound speed profile for the Pekeris model.

Figure 1. The Pekeris model

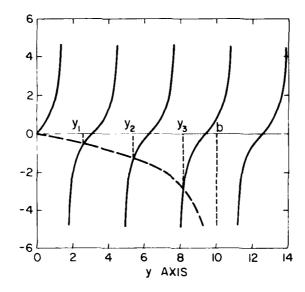


Figure 2. Graphical Solution for the Mode Eigenvalues

Graphical solution of Eq.(23), for  $\rho_2/\rho_1=2.0$  and b=10. The solid line is the tangent function. The dashed line is the function:  $-(\rho_1/\rho_2)y/[b^2-y^2)]^{1/2}$ . There are three modes in this example. The solutions  $y_n$  are indicated.

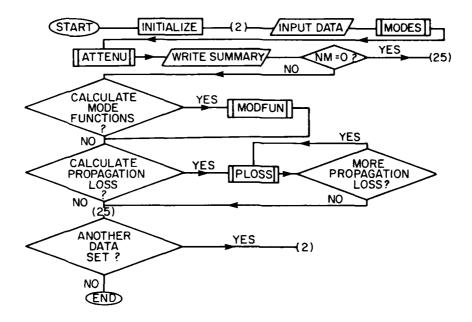


Figure 3. Simple Flowchart of NORM2L

The nodes (2) and (25) correspond to statement numbers in NORM2L.

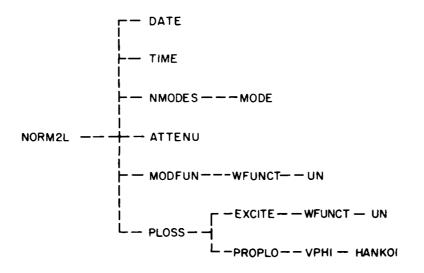


Figure 4. Tree Structure for NORM2L and its Subroutines

#### REFERENCES

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- 9. C.L. Bartberger and L.L. Ackler, "Normal mode solutions and computer programs for underwater sound propagation: Part II Program for arbitrary velocity profiles", NADC Report No. NADC-72002-AE, April 1973
- 10. Fortran Reference Manual, DEC-20-LFRMA-A-D, Digital Equipment Corporation, Maynard MA, 1976. List directed input is described on pages 10-6 and 10-7; for the DATE and TIME subroutines see pages 15-15 and 15-18.

# APPENDIX A

# USER'S GUIDE FOR PROGRAM NORM2L

- A.1 Identification
- A.2 Hardware-Software Environment
- A.3 Input/Output
- A.4 Operational Instructions
- A.5 Restrictions and Limitations
- A.6 Functions and Subroutines
- A.7 Accuracy
- A.8 Memory Requirements
- A.9 Execution Times

### A.1 Identification

Program : NORM2L

Purpose: To calculate discrete normal modes and propagation

loss for a two layer fluid acoustical model.

Author : Dale D. Ellis

Installation: Defence Research Establishment Atlantic

P.O. Box 1012 Dartmouth, N.S. Canada, B2Y 3Z7

Computer: DEC-20

Language: Fortran IV; with some minor DECsystem-20

extensions for input/output.

Date written: April 1978

Last Modification: June 1978

Present version: 3.0

Security: Unclassified

## A.2 Hardware-Software Environment

Hardware environment:

- Interactive terminal

- Line printer (optional)

Software environment:

- Interactive operating system

- FORTRAN IV compiler (with a few DEC-20 extensions for input/output statements)

- Standard Fortran library functions

- DEC-20 subroutines for date and time.

Note: None of the DEC-20 non-standard items are essential to the program; they are for convenience only and may be omitted or replaced by functions compatible with the operating system being used. The most difficult item to change will be the free-field format input and non-ANSI output, but these items are becoming quite common in FORTRAN compilers.

## A.3 Input/Output

## A.3.1 Input

Most input is list directed; that is no formatting is required [10].

The exception to this is the response to a question which requires a YES or NO answer In this case no spaces are allowed. The program checks only to see if the first character is a Y, otherwise NO is assumed.

If no change is desired to a data item (other than Y/N) a null entry (not a zero) will allow its value to remain unchanged. On the DEC-20 a comma (,) is used to signify a null entry. (Note: a carriage return by itself is ignored.)

The data items and their default values are:

Variable	Fortran name	Default value
depth of layer 1	Н	100.
sound speed in layer 1	C 1	1500.
density in layer 1	RHO 1	1.0
ratio of sound speeds	CRAT	1.2
(layer 2 to layer 1)		
ratio of densities	RHORAT	2.0
attenuation coefficient	ALPRAT	0.2
for layer 2		
frequency	FREĢ	100.
source depth	ZS	H/2.
receiver depth	ZR	H/2.
minimum range	RMIN	10000.
range increment	DELR	10000.
number of ranges	NRNG	10

The above values are typical units for isovelocity shallow water (layer 1) over a hard bottom (layer 2). The depths and ranges are in meters, the speeds in meters per second and the frequency in Hz. The attenuation coefficient is in dB/m at a frequency of 1 kHz. The attenuation is assumed to vary linearly with frequency. Units need not be metric but

should be consistent. In particular, the depths and ranges should be in the same units.

Some checking of the input parameters is performed but it is by no means exhaustive. All input parameters should be positive, except ALPRAT which may be zero. If IRHO1-1.0\>0.03 a confirmation is required. If a negative value is entered for the frequency, no calculations are performed. This enables the user who notices a previous incorrect entry to begin again. Since list directed input is used, only those values that need altering need be entered. For the others a null entry (i.e. a comma, not a zero) and carriage return will suffice.

YES/NO entries are required for control of printout and calculation of mode functions, mode excitations and propagation loss.

In the propagation loss subroutine the default values are reset each time it is called. The parameters and their default values were listed earlier. Other values may be selected and the propagation loss subroutine may be called repeatedly with different values for the source and receiver depths and range selections.

#### A.3.2 Output

Output consists of a summary of the input parameters for the calculation, the date and time, and results associated with the discrete normal modes. In the summary MODE is the mode number, KN is the mode wave number,

NORM is the normalization of the mode functions, IM(KN) is the imaginary part of the wave number and VPHASE is the phase speed. The output is normally displayed on the terminal. However, if YES is specified in answer to:

'DO YOU WANT A COPY OF THIS SUMMARY ON THE LINE PRINTER?' then all further output from the calculations of the mode functions, propagation loss and mode excitations is printed on the line printer. Only the prompting questions continue to be printed on the terminal.

The mode functions, if desired, are calculated at 12 depths equally spaced by H/10, where H is the thickness of layer one. The first line of output lists the depths. The subsequent lines list the mode functions at the corresponding depths. Note that, due to the change in density, the mode functions are discontinuous at the interface between the two layers.

The mode excitations are simply the normalized mode functions evaluated at the source depth. They may optionally be printed with the propagation loss calculation.

At each range, coherent propagation loss, incoherent propagation loss, and incoherent propagation loss with cylindrical and (approximate) near-field spherical spreading removed are calculated and printed in tabular form under the headings RANGE, COH, INCOH, and INCOH-GEOM. The propagation loss subroutine can be called repeatedly with different values for the source depth, receiver depth, and range

points. Note that each time the subroutine is called the values revert to the default values listed in the previous section.

Sample printout from a terminal is shown in Appendix

B. The underlined characters are entered by the user. Data entries are terminated by pressing the "return" key; this is indicated by <ret> on the output.

Appendix C shows the line printer output corresponding to the input shown in Appendix B. If the line printer option is not specified, this printout will appear at the terminal.

## A.4 Operational Instructions

#### Initiate:

This is an interactive program; no special instructions are necessary. For example on the DEC-20, if the program has been SAVEd as file NORM2L.EXE on the directory <ELLIS.NM>, then the command

@RUN <ELLIS.NM>NORM2L

will cause execution to begin. No system messages appear.

In the example of Appendix B the compiled program exists on file NORM2L of the user's directory, and the command

@EXECUTE NORM2L

causes the relocatable files to be linked with the system subroutines and loaded for execution. There are two lines of system messages. If only the source file NORM2L.FOR had

been on disk, then the FORTRAN compiler would have been called automatically and each subroutine name would have been typed as it was compiled.

#### Execute:

Enter data in response to questions typed on the terminal. See Appenxix A.3 for more details. As many data sets as desired may be executed.

#### Input/output data:

Both input and output appear on the terminal.

Optionally, some output may be directed to the line

printer. See Appendices B and C for an example; responses

typed by the user are underlined.

### Error procedures:

Error checking is not exhaustive although those errors that are trapped allow the user to change user input. Some warning messages are issued - see below under "Messages". The DEC-20 operating system traps overflow, square roots of negative numbers, etc., and issues warning messages for the first two errors detected. Any system error messages indicate that the results may be unreliable.

#### Interrupt:

No interrupt procedures have been coded into the program. However, on the DEC-20 typing 'control-C' once or twice will cause program execution to stop. The program can be re-run with the RUN or EXECUTE command as described in

the "Initiate" paragraph above. The START or CONTINUE commands can be used to restart the program without reloading, but these should not be used if an error has occurred.

## Terminate:

Program execution can be terminated by typing NO  $\label{eq:can_self_eq} \text{in response to the question}$ 

'DO YOU WISH TO RUN ANOTHER DATA SET ? (Y/N)'.

## Messages:

The following warning messages are issued:

Message	Explanation	Response
ARE YOU SURE ABOUT RHO1? (Y/N)	- ·	was entered correctly; a NO will cause the previous question to be repeated.
NEGATIVE FREQUENCY EXECUTION SUPPRESSED.	A negative number, either deliberately or by mistake, was entered for the frequency. No modes are calculated.	wants to run another
*** WARNING *** THERE ARE [NM] MODES. ONLY [NMAX] MODES HAVE BEEN CALCULATED.	•	None. User must decide whether the neglected modes will affect his results.

NO TRAPPED MODES.

There are no discrete modes for the current set of environmental parameters. Further calculations are skipped.

User is asked about the usual line printer summary and whether to run another data set.

CONVERGENCE NOT ACHIEVED FOR MODE [M] AFTER [MAX] ITERATIONS, DIF = [DIF].

The Newton-Raphson procedure for mode M has failed to converge to the desired tolerance after MAX iterations section 3.3 for The difference between the last two values of YN is DIF. Answers may be inaccurate.

Indicates TOL has been chosen too small, MAX not large enough, or a bug in the program. See details on how to modify TOL or MAX.

#### Restrictions and Limitations A.5

The limitations of the model are discussed in Section 2.1. This section refers to the restrictions and limitations of the program.

All input parameters must be positive; except ALPRAT which may equal zero.

The sound speed in the bottom must be greater than the sound speed in the water column; otherwise, no modes will be trapped.

The present version of the program allows for a maximum of 50 modes. This can be modified by changing a few DIMENSION statements.

A small value for the range variable may cause the Hankel function to be inaccurate. No warning is given. The error would occur at short ranges where the model is

inaccurate anyway.

The program is written in single precision. See Appendix A.7 for more comments on accuracy.

Printout of the mode functions and propagation loss appears on the line printer or terminal, but not both.

#### A.6 Functions and Subroutines

A chart of the subroutine interactions is given in Section 3.1. The program was designed to be modular for flexibility in expansion and modification; thus some duplication and inefficiency results.

The program has the following functions and subroutines. For any undefined variables see Section 3.2.

## 1. subroutine NMODES (H, HOMC, CRAT, RHO1, RHORAT, NM, AKM, ANM)

- given the input environmental parameters H, HOMC, CRAT, RHO1, and RHORAT, calculates the number of trapped modes (NM), the wave numbers of the modes (array AKM), and the normalization factors for the wave functions of each mode.

#### 2. subroutine MODE (M, YO, BSQ, RHORAT, YN, IER)

- uses a Newton-Raphson iteration procedure to calculate YN, which gives the M-th normal mode eigenvalue [see Eqs. 29-31]. YO is an initial guess, BSQ and RHORAT some needed input variables, and IER an output error parameter in case the method fails to converge to the required tolerance.

#### 3. subroutine ATTENU

- calculates the imaginary part of the wave number for the modes due to the bottom attenuation using a perturbation formula. Parameters are passed using labelled common.

## 4. subroutine MODFUN (NM, IO)

- calculates and prints (on logical unit number IO) the NM eigenfunctions evaluated at the 12 depths equally spaced at intervals of one tenth the thickness of layer one. This subroutine should be generalized in future versions.

## 5. subroutine WFUNCT (N, NPT, DZ, ZVALS, WVALS, ICH)

- evaluates and stores in array WVALS the mode function for the N-th mode at the NPT depths stored in array ZVALS. If ICH is non-zero the array ZVALS is calculated: ZVALS(I)=(I-1)\*DZ. The mode parameters are obtained via labelled common.

## 6. function UN (Z,N,H,C1,C2,RHORAT,CMEGA,NM,AKM, ANM)

 $\,$  – evaluates the N-th mode function at depth Z. The other parameters are required for calculation of the mode function.

#### 7. subroutine PLOSS (IO)

- input/output subroutine for propagation loss calculations. IO is the logical number of the file on which the results are written.

#### 8. subroutine EXCITE (ZS, EX, NM)

- calculates the mode excitations (array EX) for source depth ZS for the first NM modes.

#### 9. function PROPLO (R, ZR, ZS, COHI, RCOHI)

- for range R, receiver depth ZR, and source depth ZS, calculates the coherent propagation loss PROPLO, the incoherent propagation loss COHI, and incoherent propagation loss RCOHI with cylindrical and near-field spherical spreading removed. All propagation losses are in dB referenced to unit distance.

#### 10. complex function VPHI (R,ZR,ZS,VPHI2)

- evaluates the velocity potential VPHI and the square of the incoherent velocity potential VPHI2, for range R, receiver depth ZR and source depth ZS.

#### 11. complex function HANKO1 (RK)

- evaluates the asymptotic Hankel function of the zeroth order and first kind for large values of RK.

The following DEC-system routines are used [10]. They are not essential to the calculations and are used to uniquely label the results.

#### 1. subroutine DATE (DDMMYY)

- places the current date as left-justified ASCII characters into a two-word array DDMMYY. The date is of the form dd-mmm-yy, where dd is a two-digit day (if the first digit is zero, it is converted to a blank), mmm is a three-character month and yy is a two-digit year; e,g. 31-Mar-78.

#### 2. subroutine TIME (HHMM)

- returns the current time in HHMM as left-justified ASCII characters in the form hh:mm, where hh is the hours in 24-hour time and mm is the minutes.

#### A.7 Accuracy

The program and subroutines are written in single precision, so the accuracy is machine dependent to some extent. The DEC-20 has 36-bit words, or about 8 digits accuracy for floating point numbers.

With the tolerance on the eigenvalue set at 1.0E-8, the wave numbers seem to be correct to 8 significant figures, the mode functions seem correct to 6 significant figures, and for the non-attenuated case the propagation loss seems correct to about 4 significant digits. More extensive comparisons are made in section 3.3. In all cases

tried so far, convergence has occurred in fewer than 20 iterations.

Since only three terms are used in the expression for the Hankel function, propagation loss may be inaccurate at short ranges, on the order of several water depths.

However, the normal mode model is inaccurate at these ranges anyway.

## A.8 Memory Requirements

The .EXE file requires 13 pages or 6656 36-bit words on the DEC-20.

The present version of the program has 461 lines of code, a total of 12945 ASCII characters.

#### A.9 Execution times

The execution time depends more or less linearly on the number of modes calculated. The number of modes (see Eq. 26) in turn depends linearly on the frequency and on the thickness of layer one. The number of modes also increases with the sound speed ratio CRAT.

For the calculation of Appendices B and C, with seven modes and all options in effect, one and one-half to three CPU seconds execution time is used on the DEC-20. The exact execution time depends on the system load.

# APPENDIX B SAMPLE TERMINAL INPUT/OUTPUT

All user entries are underlined. The symbol  $\langle r\underline{e}t \rangle$  indicates that the user must press the "return" key to terminate the data entry. The line printer output associated with this example is given in Appendix C.

@EXECUTE NORM2L <ret>

LINK: Loading

[LNKXCT NORM2L Execution]

14-Jun-79 09:30

## NORMAL MODE TWO LAYER MODEL

WATER DEPTH ? 100 <ret>

FIRST LAYER: C1, RHO1 ?

1500, 1. (ret)

SECOND LAYER RATIOS: CRAT, RHORAT ?

1.2. 2.0 (ret)

C2,RHO2: 1800.000 2.0

ATTENUATION IN DB/UNIT LENGTH // 1 KHZ ?

<u>0.2</u> (ret)

FREQUENCY ? 100 <ret>

14-Jun-79 09:30

#### NORMAL MODE TWO LAYER MODEL

WATER DEPTH 100.0

C1, RHO1 1500.00 1.0000 C2, RHO2 1800.00 2.0000 CRAT, RHORAT 1.2000 2.0000

FREQUENCY 100.00

ALPRAT 0.2000 DB/UNIT DISTANCE // 1 KHZ ATTN 0.00230 UNITS OF INVERSE DISTANCE

7 MODES CALCULATED

MODE	KN	NORM	VPHASE	IM(KN)
1	0.41787760	0.135884	1503.5947	0.23081E-05
2	0.41483675	0.136394	1514.6163	0.85045E-05
3	0.40965783	0.137016	1533.7642	0.17149E-04
<u>L</u>	0.40220081	0.137577	1562.2010	0.27377E-04
5	0.39229571	0.137972	1601.6451	0.39711E-04
O	0.37974394	0.138101	1654.5847	0.57252E-04
7	0.36434072	0.137587	1724.5356	0.94016E-04

DO YOU WANT A COPY OF THIS SUMMARY ON THE LINE PRINTER ? TYPE YES OR NO.

<u>Y</u> <ret>

CALCULATE MODE FUNCTIONS ? (Y/N).

Y <ret>

CALCULATE PROPAGATION LOSS ? (Y/N).

<u>Y</u> <ret>

CHANGE DEFAULT VALUES ? (Y/N).

<u>N</u> <ret>

CALCULATE EXCITATIONS OF EACH MODE ? (Y/N)

<u>Y</u> <ret>

MORE PROPAGATION LOSS CALCULATIONS ? (Y/N).

<u>Y</u> <ret>

CHANGE DEFAULT VALUES ? (Y/N).

<u>Y</u> <ret>

SOURCE DEPTH, RECEIVER DEPTH ?

25. (ret)

RMIN, DELR, NRNG ?

... <ret>

CALCULATE EXCITATIONS OF EACH MODE ? (Y/N)

<u>Y</u> <ret>

MORE PROPAGATION LOSS CALCULATIONS ? (Y/N).

<u>N</u> <ret>

RUN ANOTHER DATA SET ? (Y/N).

<u>N</u> <ret>

END OF EXECUTION

CPU TIME: 2.09 ELAPSED TIME: 1:13.20

EXIT

ø

# APPENDIX C SAMPLE LINE PRINTER OUTPUT

The output shown here was generated by the terminal session illustrated in Appendix B.

# 14-Jun-79 09:30

## NORMAL MODE TWO LAYER MODEL

WATER DEPTH C1, RHO1 C2, RHO2 CRAT, RHORAT	100.0 1500.00 1800.00 1.2000	1.0000 2.0000 2.0000	
FREQUENCY	100.00		
ALPRAT ATTN	0.2000 0.00230	DB/UNIT DISTANCE UNITS OF INVERSE	

## 7 MODES CALCULATED

MODE	KN	NORM	VPHASE	IM(KN)
1	0.41787760	0.135884	1503.5947	0.23081E-05
2	0.41483675	0.136394	1514.6163	0.85045E-05
3	0.40965783	0.137016	1533.7642	0.17149E-04
4	0.40220081	0.137577	1562.2010	0.27377E-04
5	0.39229571	0.137972	1601.6451	0.39711E-04
6	0.37974394	0.138101	1654.5847	0.57252E-04
7	0.36434072	0.137587	1724.5356	0.94016E-04

## MODE WAVE FUNCTIONS

DEPTHS 10.00000 50.00000 90.00000	20.00000 60.00000 100.0000	30.00000 , 70.00000 , 110.0000 ,	40.00000 , 80.00000 , 120.0000 ,
MODES			
1			
0.3878757E-01,	0.7434761E-01	0.1037211	0.1244640 ,
0.1348502 ,	0.1340154	0.1220292	0.9988882E-01,
0.6943669E-01,			0.1678062E-03,
0.7480736E-01,	0.1251040	0.1344102	0.9967681E-01,
	-0.4568638E-01		-0.1360775
-0.1188813 ,		, -0.3334304E-02,	-0.3544382E-03,
0.1050843 .	0.1348664	0.6800471E-01,	-0.4758839E-01,
		-0.2245802E-01,	0.8925168E-01,
0.1370046 ,		0.5072421E-02,	

```
4
0.1266855 , 0.9880192E-01, -0.4962995E-01, -0.1375083 ,
-0.5761266E-01, 0.9257621E-01, 0.1298128 , 0.8664670E-02,
-0.1230552 , -0.1046353 , -0.7094869E-02, -0.9621448E-03,
5
0.1372500 , 0.2804273E-01, -0.1315203 , -0.5491478E-01,
0.1203002 , 0.7949435E-01, -0.1040581 , -0.1007553 ,
0.8347185E-01, 0.1178102 , 0.9832619E-02, 0.1641291E-02,
6
0.1354279 , -0.5303766E-01, -0.1146567 , 0.9794070E-01,
0.7630017E-01, -0.1278222 , -0.2624115E-01, 0.1380990 ,
-0.2784262E-01, -0.1271950 , -0.1425772E-01, -0.3196392E-02,
7
0.1210085 , -0.1151735 , -0.1138861E-01, 0.1260130 ,
-0.1085481 , -0.2269905E-01, 0.1301526 , -0.1011776 ,
-0.3385370E-01, 0.1333989 , 0.2348356E-01, 0.8268099E-02,
```

1 0.13485018

	2 0.32284186E 3 -0.12908018 4 -0.57612656E 5 0.12030022 6 0.76300173E 7 -0.10854806	-01	
SOURCE DEPTH	50.00 R	ECEIVER DEPTH	50.00
RANGE	P.L. (DB RE	UNIT DISTANCE) INCOH	INCOH-GEOM
10000.00 20000.00 30000.00 40000.00 50000.00 70000.00 80000.00 90000.00	, 58.37791 , 64.97957 , 65.42920 , 70.69642 , 76.35365 , 75.91258 , 74.76040 , 74.88633 , 74.89706 , 74.40432	60.02504 64.23382 ,66.82623 ,68.70615 ,70.17996 ,71.39203 ,72.42286 ,73.32203 ,74.12217 ,74.84582	0.2504134E-01, 1.223522, 2.055018, 2.685551, 3.190257, 3.610515, 3.971880, 4.291131, 4.579747, 4.845824,

MODE EXCITATIONS SOURCE DEPTH = 50.00

#### PROPAGATION LOSS

40000.00

50000.00

60000.00

70000.00

80000.00

90000.00

100000.0

		MODE EXC	OLTATION	IS	SOU	RCE DEPTH =	25.00
		1 0.899	75154E-	-01			
		2 0.135	42200				
		3 0.111					
			91923E-	-01			
		5 -0.6969	-	-01			
		6 -0.132	22866				
		7 -0.123	51683				
SOURCE DEPTH		25.00	RE	CCEIVER I	DEPTH	50.00	
RANGE		P.L.	(DB RE	UNIT DIS	STANCE)		
		COH		INCOH		INCOH-GEOM	
10000.00	,	67.96269	,	62.0932	2,	2.093222	•
20000.00		66.87508	•	66.65010	0 .	3.639804	
30000.00	· ·	71.06421		69.42610	6 .	4.654949	

73.10997

69.76201

70.69862

72.88694

75.62021

78.87690

80.43400

71.44136

73.03228

74.34834

75.47003

76.44690

77.31236

78.09026

5.420760

6.042584

6.566830

7.019045

7.416999

7.769934

8.090258

# APPENDIX D PROGRAM LISTING

```
PROGRAM NORM2L
С
С
   TWO LAYER NORMAL MODE PROGRAM
\mathbb{C}
\mathsf{C}
        AUTHOR: DALE D. ELLIS
С
                DEFENCE RESEARCH ESTABLISHMENT ATLANTIC
C
                 DARTMOUTH, NOVA SCOTIA, CANADA
C
C
        DATE WRITTEN: APRIL 1978
C
        LAST MODIFICATION: JUNE 1978
C
             ( SOME COSMETIC CHANGES SINCE THEN)
C
        VERSION: 3.0
                         MOD 41
С
        COMPUTER: DEC-20/40
C
        OPERATING SYSTEM: TOPS-20
C
C
        LANGUAGE: FORTRAN IV, WITH A FEW DEC-SYSTEM EXTENSIONS
С
С
С
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      COMMON /EIGENF/ NM, AKM(50), ANM(50), ATN(50)
      COMMON /CNTLNM/ MAX, TOL, NMIN, NMAX, VMIN, VMAX
      COMMON /CNTLIO/ II, IO, IT
      DIMENSION DDMMYY(2)
      DATA H,C1,RHO1,CRAT,RHORAT,ALPRAT,FREQ/100.,1500.,1.,1.2
     1, 2.0,0.2,100. /
      DATA II, IO, IT /5,3,5/
      DATA TOL /1.E-8/, MAX/20/, NMIN/1/, NMAX/50/
      DATA NCALL/0/
С
      PI2 = 8.*ATAN(1.)
      ISAVE=10
      DBNP=ALOG(10.)/20.
      CALL DATE (DDMMYY)
      CALL TIME (HHMM)
      WRITE (IT,500) DDMMYY,HHMM
500
      FORMAT (1X,2A5,5X,A5)
С
         INPUT DATA
С
    2 CONTINUE
С
      WRITE (IT.400)
400
      FORMAT (///,11X,28H NORMAL MODE TWO LAYER MODEL )
C
      WRITE (IT, 401)
401
      FORMAT (///,14H WATER DEPTH ?)
      READ (II,*) H
    4 WRITE (IT,402)
402
      FORMAT (24H FIRST LAYER: C1,RHO1 ? )
      READ (11,*) C1,RHO1
```

```
IF(ABS(RHO1-1.) .LT.0.03) GO TO 5
      WRITE(IT,412)
412
      FORMAT (' ARE YOU SURE ABOUT RHO1 ? (Y/N).')
      READ (II, 302) YESNO
      IF(YESNO.NE.1HY) GO TO 4
   5 WRITE (IT,403)
403
      FORMAT (36H SECOND LAYER RATIOS: CRAT, RHORAT?)
      READ (II, *) CRAT, RHORAT
      IF (CRAT.GT.1.) GO TO 6
      WRITE (IT, 417)
417
      FORMAT (' CRAT=C2/C1 MUST BE GREATER THAN 1.0. ENTER NEW VALUE.')
      GO TO 5
    6 RHO2 = RHO1*RHORAT
      C2 = CRAT * C1
      WRITE (IT, 404) C2, RHO2
404
      FORMAT (22X,10HC2,RHO2: ,F10.3,F10.1,/)
С
      WRITE (IT, 406)
406
      FORMAT (' ATTENUATION IN DB/UNIT LENGTH // 1 KHZ ?')
      READ (II, *) ALPRAT
      WRITE (IT, 405)
405
      FORMAT (12H FREQUENCY ?)
      READ (II,*) FREQ
      OMEGA =PI2*FREQ
      IF (FREQ.LT.O.) WRITE (IT,413)
413
      FORMAT (' NEGATIVE FREQUENCY. EXECUTION SUPPRESSED.')
      IF (FREQ.LT.O.) GO TO 25
С
      HOMC= H*OMEGA/C1
      AK1 = OMEGA/C1
      AK2 = OMEGA/C2
      ATTN=DBNP*(ALPRAT*FREQ/1000.)
С
      CALL NMODES (H, HOMC, CRAT, RHO1, RHORAT, NM, AKM, ANM)
С
      IF (NM.LE.NMAX) GO TO 8
      WRITE (IT, 419) NM, NMAX
      FORMAT(//, * *** WARNING ***
                                       THERE ARE', 15, ' MODES',/
     1,' ONLY', 15,' MODES HAVE BEEN CALCULATED.')
      NM=NMAX
    8 IF (NM.GT.O.) CALL ATTENU
      10=IT
      IC=0
    9 CONTINUE
      IF(NCALL.NE.O) WRITE (IO.499)
      FORMAT(1H1)
      WRITE (10,500) DDMMYY, HHMM
      WRITE (10,400)
      WRITE (IO,501) H,C1,RHO1,C2,RHO2,CRAT,RHORAT,FREQ
     1, ALPRAT, ATTN
      WRITE (10,507) NM
```

```
507
      FORMAT (/, 15, ' MODES CALCULATED')
      IF (NM.LT.1) GO TO 13
      WRITE (10,510)
510
     FORMAT (//,6H MODE,7X,2HKN,13X,4HNORM,10X,6HVPHASE,9X,
     1 6HIM(KN) )
      DO 11 I=1,NM
      VPHASE=OMEGA/AKM(I)
      WRITE (IO,301) I,AKM(I),ANM(I),VPHASE,ATN(I)
   11 CONTINUE
301
     FORMAT (15,G17.8,G15.6,G16.8,G13.5)
      FORMAT (12H-WATER DEPTH,F10.1,/,12H C1, RHO1
501
                                                      ,F11.2,
     1 F11.4,/,12H C2, RHO2 ,F11.2,F11.4,/12H CRAT,RHORAT,
     2 F13.4,F9.4,//,12H FREQUENCY ,F11.2 ,
        //,7H ALPRAT,F18.4,'
                               DB/UNIT DISTANCE // 1 KHZ',
     4 /,5H ATTN, 11X, F10.5, UNITS OF INVERSE DISTANCE')
   13 IF (IC.EQ.1) GO TO 15
     WRITE (IT, 407)
407
      FORMAT (//, ' DO YOU WANT A COPY OF THIS SUMMARY ON THE LINE',
     1' PRINTER ?',/,10X,'TYPE YES OR NO.')
      READ (IT, 302) YESNO
302
      FORMAT (A1)
      IF (YESNO.NE.1HY) GO TO 15
      IO=ISAVE
      IC=1
      NCALL=NCALL+1
      GO TO 9
              CONTINUE
      IF (NM.LT.1) GO TO 25
C
        IO=ISAVE
      WRITE (IT, 408)
408
      FORMAT (' CALCULATE MODE FUNCTIONS ? (Y/N).')
      READ (IT, 302) YESNO
      IF (YESNO.NE.1HY) GO TO 20
      CALL MODFUN (NM, IO)
   20 WRITE (IT,409)
409
      FORMAT( ' CALCULATE PROPAGATION LOSS ? (Y/N).')
      READ (IT, 302) YESNO
      IF (YESNO.NE.1HY ) GO TO 25
   22 CALL PLOSS (IO)
      WRITE (IT, 415)
415
      FORMAT (' MORE PROPAGATION LOSS CALCULATIONS ? (Y/N).')
      READ (IT, 302) YESNO
      IF (YESNO.EQ.1HY) GO TO 22
   25 WRITE (IT,410)
      FORMAT(' RUN ANOTHER DATA SET ? (Y/N).')
      READ (IT, 302) YESNO
      CALL TIME (HHMM)
      IF (YESNO.EQ.1HY) GO TO 2
      END
```

```
SUBROUTINE NMODES (H, HOMC, CRAT, RHO1, RHORAT, NM, AKM, ANM)
С
   NORMAL MODE CALCULATION FOR TWO LAYERS
С
С
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
С
      COMMON /CNTLNM/MAX, TOL, NMIN, NMAX, VMIN, VMAX
      COMMON /CNTLIO/ II, IO, IT
      LOGICAL EXTRA
      DIMENSION AKM(NM), ANM(NM)
      DATA PI /3.14159265 /
      DATA EXTRA /.FALSE./
      BSQ = HOMC **2 * (1.-1./CRAT**2)
         = SQRT (BSQ)
      NM = B/PI + 0.5
      IF (NM.LT.1) GO TO 40
      NMX = MINO (NM, NMAX)
      YO = (NMIN-1.25)*PI
      DO 20 M =NMIN,NMX
      YO = YO + PI
      IF(EXTRA) WRITE(IT,410) M
410
      FORMAT (5HOMODE, 15)
      IM = M
      CALL MODE (IM, YO, BSQ, RHORAT, YN, IER)
      RKNSQ= (HOMC##2-YN##2)/H##2
      RKN = SQRT (RKNSQ)
      AKM(M) = RKN
      GM1H = YN
      GM2H = SQRT (BSQ-YN**2)
      AM2 = 2./H/RHO1/(1.-SIN(2.*GM1H)/(2.*GM1H) + (SIN (GM1H))
     1**2/(RHORAT*GM2H))
      ANM(M)=SQRT(AM2)
      IF (EXTRA) WRITE (IT,*) YN, AKM(M), ANM(M)
   20 CONTINUE
\mathbb{C}
      RETURN
C
   40 WRITE(1T, 420)
      FORMAT (17H NO TRAPPED MODES )
420
      RETURN
      END
```

```
SUBROUTINE MODE (M, YO, BSQ, RHORAT, YN, IER)
C
C OBTAINS YM FOR M-TH MODE USING NEWTON-RAPHSON PROCEDURE
С
С
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
      LOGICAL EXTRA
      COMMON /CNTLNM/ MAX, TOL, NMIN, NMAX, VMIN, VMAX
      COMMON /CNTLIO/ II, IO, IT
      DATA PI /3.14159265358979/
      DATA EXTRA /.FALSE./
      IER=0
      B=SQRT(BSQ)
      R21B=(RHORAT**2-1.)/BSQ
      PIM=PI*M
      YMAX=AMIN1(PIM,B)
      YMIN=PI*(M-0.5)
      YM=YO
      IF (YM.GT.YMAX.OR.YM.LT.YMIN) YM=(YMIN+YMAX)/2.
С
      DO 10 1=1,MAX
      SRBY = SQRT (BSQ-YM^{**}2)
      FY = YM-PIM + ATAN (RHORAT*YM/SRBY)
      DF = 1. + RHORAT/SRBY/(1. + R21B*Y**2)
      YN = YM-FY/DF
      DIF= YN-YM
      IF (EXTRA) WRITE(IT,*) YM,FY,DF,YN,DIF
      IF (ABS(DIF/YN).LT. TOL) GO TO 15
      YM=YN
      IF (YM.LT.YMIN) YM=YMIN
      IF (YM.GT.YMAX) YM=YMAX
   10 CONTINUE
C
      WRITE (IT, 410) M, MAX, DIF
     FORMAT (34H CONVERGENCE NOT ACHIEVED FOR MODE ,13,/,10X,
     1 5HAFTER, 13, 19H ITERATIONS DIF =, E12.4)
      IER=1
      RETURN
   15 CONTINUE
      RETURN
      END
```

```
SUBROUTINE ATTENU
С
C BOTTOM ATTENUATION USING INGENTO'S PERTURBATION FORMULA
С
С
        WRITTEN BY DALE D ELLIS
                                       APRIL 1978
С
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      COMMON /EIGENF/ NM, AKM(50), ANM(50), ATN(50)
С
      IF (ATTN.EQ.O.) GO TO 20
      CONST=0.5*ATTN*OMEGA*RHO1/C2/RHORAT
С
      DO 10 I=1,NM
      ATN(I) = CONST^{*}(ANM(I)^{*}SIN(H^{*}SQRT(AK1^{**}2-AKM(I)^{**}2)))^{**}2
     1 / (AKM(I)*SQRT(AKM(I)**2-AK2**2) )
   10 CONTINUE
      RETURN
C
          NO ATTENUATION
   20 DO 21 I=1,NM
   21 ATN(I)=0.
      RETURN
      END
```

```
SUBROUTINE MODFUN (NM, IO)
С
С
   INPUT/OUTPUT ROUTINE FOR MODE FUNCTION CALCULATIONS
С
С
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
С
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      DIMENSION ZVALS(100), WVALS(100)
      WRITE (10,430)
430
      FORMAT(///, 10X, 'MODE WAVE FUNCTIONS',/)
      NPT=12
      IN=1
      DZ=H/10.
      CALL WFUNCT (1,NPT,DZ,ZVALS,WVALS,0)
      WRITE (10,431)
431
      FORMAT (' DEPTHS')
      WRITE (IO,*) (ZVALS(I),I=1,NPT)
      WRITE (10,432)
      FORMAT (/, ' MODES')
432
      WRITE (10,202) IN
202
      FORMAT (13)
      WRITE (IO, *) (WVALS(I), I=1, NPT)
      IF (NM.LT.2) RETURN
      DO 10 IN=2,NM
      INN=IN
      CALL WFUNCT (INN, NPT, DZ, ZVALS, WVALS, 0)
      WRITE (10,202) INN
      WRITE (IO, *) (WVALS(I), I=1, NPT)
   10 CONTINUE
      RETURN
      END
```

```
SUBROUTINE WFUNCT (N, NPT, DZ, ZVALS, WVALS, ICH)
С
C EVALUATES MODE FUNCTIONS AT A NUMBER OF DEPTHS
С
С
        WRITTEN BY DALE D ELLIS
                                     APRIL 1978
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      COMMON /EIGENF/ NM, AKM(50), ANM(50), ATN(50)
      DIMENSION ZVALS(NPT), WVALS(NPT)
      IF (ICH.NE.O) GO TO 10
      DO 4 I=1,NPT
    4 ZVALS (1)=DZ*I
   10 CONTINUE
      DO 14 I=1,NPT
      WVALS(I) = UN (ZVALS(I),N,H,C1,C2,RHORAT,OMEGA,NM,AKM,ANM )
   14 CONTINUE
      RETURN
      END
      FUNCTION UN (Z,N,H,C1,C2,RHORAT,OMEGA,NM,AKM,ANM)
C N-TH NORMAL MODE EVALUATED AT DEPTH Z
С
        WRITTEN BY DALE D ELLIS
                                     APRIL 1978
С
      DIMENSION AKM(NM), ANM(NM)
      IF (N.GT.NM) GO TO 13
      GM1=SQRT ( (OMEGA/C1)**2 - AKM(N)**2 )
      IF (Z.GT.H) GO TO 4
      UN = ANM(N)*SIN (GM1*Z)
      RETURN
    4 UN=1./RHORAT*ANM(N)*EXP(-(Z-H)*SQRT(AKM(N)**2-(OMEGA/C2)**2))
     1 * SIN (GM1*H)
      RETURN
   13 UN=0.
      RETURN
      END
```

```
SUBROUTINE PLOSS (IO)
   INPUT/OUTPUT ROUTINE FOR PROPAGATION LOSS CALCULATIONS
С
        WRITTEN BY DALE D ELLIS
                                       APRIL 1978
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      COMMON /EIGENF/ NM, AKM(50), ANM(50), ATN(50)
      COMMON /CNTL10/ II, ION, IT
      DIMENSION EX(50)
      WRITE (10,440)
440
      FORMAT (///, ' PROPAGATION LOSS'/)
      ZS=H/2.
      ZR=H/2.
      RMIN=10000.
      DELR=10000.
      NRNG = 10
      WDEPTH= 10.*ALOG10(H)
      WRITE (IT, 434)
434
      FORMAT (' CHANGE DEFAULT VALUES ? (Y/N).')
      READ(IT, 435) YESNO
435
      FORMAT (A1)
      IF(YESNO.NE.1HY) GO TO 6
      WRITE (IT, 436)
436
      FORMAT (' SOURCE DEPTH, RECEIVER DEPTH ?')
      READ (IT, *) ZS, ZR
      WRITE (IT, 437)
437
      FORMAT (' RMIN, DELR, NRNG ?')
      READ (IT,*) RMIN, DELR, NRNG
С
    6 CONTINUE
      WRITE (IT,438)
      FORMAT (' CALCULATE EXCITATIONS OF EACH MODE ? (Y/N)')
      READ (IT, 435) YESNO
      IF (YESNO.NE.1HY) GO TO 8
      CALL EXCITE (ZS, EX, NM)
      WRITE (10,439) ZS
439
      FORMAT (20X, 'MODE EXCITATIONS', 10X, 'SOURCE DEPTH =',G11.4)
      WRITE (IO, 444) (I, EX(I), I=1, NM)
444
      FORMAT (15X, 15, G17.8)
    8 CONTINUE
C
      WRITE (10,441) ZS,ZR
441
      FORMAT (/,13H SOURCE DEPTH,F10.2,10X,14HRECEIVER DEPTH,
     1 F10.2,//,5X,5HRANGE,13X,'P.L. (DB RE UNIT DISTANCE)')
      WRITE (JU, 442)
442
      FORMAT (2:X,'COH', 12X,'INCOH', 9X,'INCOH-GEOM')
      DO 10 IR=1,NRNG
      R=RMIN+(IR-1)*DELR
      PL=PROPLO (R,ZR,ZS,COHI,RCOHI)
      GCOHI=RCOHI-WDEPTH
```

```
WRITE (10,*) R,PL,COHI,GCOHI
   10 CONTINUE
      RETURN
      END
      SUBROUTINE EXCITE (ZS, EX, NMD)
C CALCULATES MODE EXCITATIONS (I.E. MODE FUNCTION AT SOURCE DEPTH)
\mathsf{C}
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
С
      DIMENSION EX(NMD)
      DO 10 I = 1, NMD
      II=I
      CALL WFUNCT (II,1,DZ,ZS,EX(II),1)
   10 CONTINUE
      RETURN
      END
      FUNCTION PROPLO (R,ZR,ZS,COHI,RCOHI)
С
С
  PROPAGATION LOSS IN DB
С
С
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
С
        REVISED JUNE 1979 - QUANTITIES MADE POSITIVE
      COMPLEX VPHI, V
      V = VPHI (R, ZR, ZS, VCOHI)
      VMOD = V*CONJG (V)
      PROPLO= -10. *ALOG10 (VMOD)
      COHI = -10.*ALOG10(VCOHI)
      RCOHI = -10.*ALOG10(R*VCOHI)
      RETURN
      END
```

```
COMPLEX FUNCTION VPHI (R, ZR, ZS, COHI)
С
   VELOCITY POTENTIAL FOR PROPAGATION LOSS CALCULATIONS
    ALLOWS RECEIVER DEPTH ZR TO BE GREATER THAN WATER DEPTH H
С
        WRITTEN BY DALE D ELLIS
                                      APRIL 1978
С
      COMPLEX HANKO1, HK, TERM
      DOUBLE PRECISION SUMR, SUMI
      COMMON /ENVIRN/ H,C1,RHO1,C2,RHORAT,ATTN,OMEGA,AK1,AK2
      COMMON /EIGENF/ NM, AKM(50), ANM(50), ATN(50)
      DATA PI/3.14159265/
С
      SUMR=0.DO
      SUMI=0.D0
      COHI=0.
      DO 10 I=1, NM
      HK=HANKO1(AKM(I)*R)
      GM1=SQRT (AK1**2-AKM(I)**2)
      UNS =SIN (ZS*GM1) *ANM(I)
      ALOSS=EXP(-ATN(I)*R)
      IF(ZR.GT.H) GO TO 6
      UNR =SIN (ZR*GM1) *ANM(I)
      GO TO 8
    6 GM2= SQRT (AKM(I)**2-AK2**2)
      UNR =1./ RHORAT*ANM(I)*EXP(-(ZR-H)*GM2) * SIN (GM1*H)
    8 SUMR = SUMR + UNS*UNR*ALOSS*REAL(HK)
      SUMI = SUMI + UNS*UNR*ALOSS*AIMAG(HK)
      TERM=(UNS*UNR*ALOSS)*HK
      COHI=TERM*CONJG(TERM) + COHI
   10 CONTINUE
С
      VPHI = CMPLX(0.,PI)*CMPLX(SNGL(SUMR),SNGL(SUMI))
      COHI=PI**2 * COHI
      RETURN
      END
```

```
COMPLEX FUNCTION HANKO1(Z)

C ASYMPTOTIC HANKEL FUNCTION OF FIRST KIND AND ZEROTH ORDER

C WRITTEN BY DALE D ELLIS APRIL 1978

C DATA PI /3.14159265/
CHI = Z - PI/4.
P = 1. - (9./128.)/Z**2
Q = -1./(8*Z)

C HANKO1 = SQRT(2./(PI*Z))*CMPLX(P,Q)*CMPLX(COS(CHI),SIN(CHI))
RETURN
END
```

#### APPENDIX E

### FUTURE MODIFICATIONS AND EXTENSIONS

Some suggested improvements and extensions to the present program are listed below.

- 1. Make optional instructions available to the user at the beginning of program execution.
- 2. Type the current value of the data item to be entered. For example, the first question might read: 'WATER DEPTH 100. ?'
- 3. Add a subroutine CHOICE to allow the user to modify some of the control parameters in the COMMON block /CNTLNM/. For the option of starting the calculations at a mode number greater than 1, some subroutines would need modification.
- \*4. Improve the Hankel function to maintain accuracy near the source. Type a warning message when the function is not sufficiently accurate.
- 5. Generalize MODFUN to handle an arbitrary number of specified depths. The subroutines called by MODFUN are sufficiently general to handle this possibility.
- 6. Add the possibility of the optional printout appearing on both the line printer and terminal.
- \*7. Calculate the group velocity, cutoff frequency, and equivalent ray angle for each mode.
- \*8. Optionally display the mode functions and propagation loss, either as a line printer plot or a proper graph.

<sup>\*</sup> These items have been included in a newer version of NORM2L - PEKRIS - which is still undergoing development.

It is hoped to try some new ideas using NORM2L or a revised version of it.

- 1. Incorporate range dependent normal mode theory, at least in the adiabatic approximation.
- 2. Include the effects of scattering from a rough surface or bottom.
- 3. Add the effects of continuous modes. This is necessary if pressure or propagation loss is needed near the source.
- 4. Create a similar program in which the bottom layer will also support shear waves.
- 5. Already parts of the program have been modified and used in a problem involving mode enhancement [4], and for debugging a general normal mode program [3]. These uses were not foreseen at the time of writing the program.

# APPENDIX F

## USER COMMENTS

This space is provided for the user to add his notes or comments. Any suggestions for improvements or additions will be considered by the author for implementation in future versions of NORM2L.

AD-A096 548

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